

2.4 — Stackelberg Competition

ECON 316 • Game Theory • Fall 2021

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Models of Oligopoly



Three canonical models of Oligopoly

1. Bertrand competition

- Firms **simultaneously** compete on **price**

2. Cournot competition

- Firms **simultaneously** compete on **quantity**

3. Stackelberg competition

- Firms **sequentially** compete on **quantity**



Stackelberg Competition



Henrich von Stackelberg

1905-1946

- "**Stackelberg competition**": Cournot-style competition, two (or more) firms compete on **quantity** to sell the **same good**
- Again, firms' joint output determines the market price faced by all firms
- But firms set their quantities **sequentially**
 - **Leader** produces first
 - **Follower** produces second

Stackelberg Competition: Example



Example: Return to **Saudi Arabia** (sa) and **Iran** (i), again with the market (inverse) demand curve:

$$P = 200 - 3Q$$

$$Q = q_{sa} + q_i$$

- We solved for Saudi Arabia and Iran's **reaction functions** in **Cournot competition** last class:

$$q_{sa}^* = 30 - 0.5q_i$$

$$q_i^* = 30 - 0.5q_{sa}$$

Stackelberg Competition: Example



$$q_{sa}^* = 30 - 0.5q_i$$

$$q_i^* = 30 - 0.5q_{sa}$$

- Suppose **Saudi Arabia** is the **Stackelberg leader** and produces q_{sa} **first**
- Saudi Arabia knows exactly how Iran will respond to its output

$$q_i^* = 30 - 0.5q_{sa}$$

- **Saudi Arabia**, as leader, essentially faces **entire market demand**
 - But **can't** act like a pure monopolist!
 - knows that **follower** will still produce afterwards, which pushes down market price for both firms!

Stackelberg Competition: Example



- Substitute **follower's** reaction function into (inverse) market demand function faced by **leader**

$$P = 200 - 3q_{sa} - 3(30 - 0.5q_{sa})$$

$$P = 110 - 1.5q_{sa}$$

- Now find $MR(q)$ for **Saudi Arabia** from this by doubling the slope:

$$MR_{Leader} = 110 - 3q_{sa}$$

Stackelberg Competition: Example



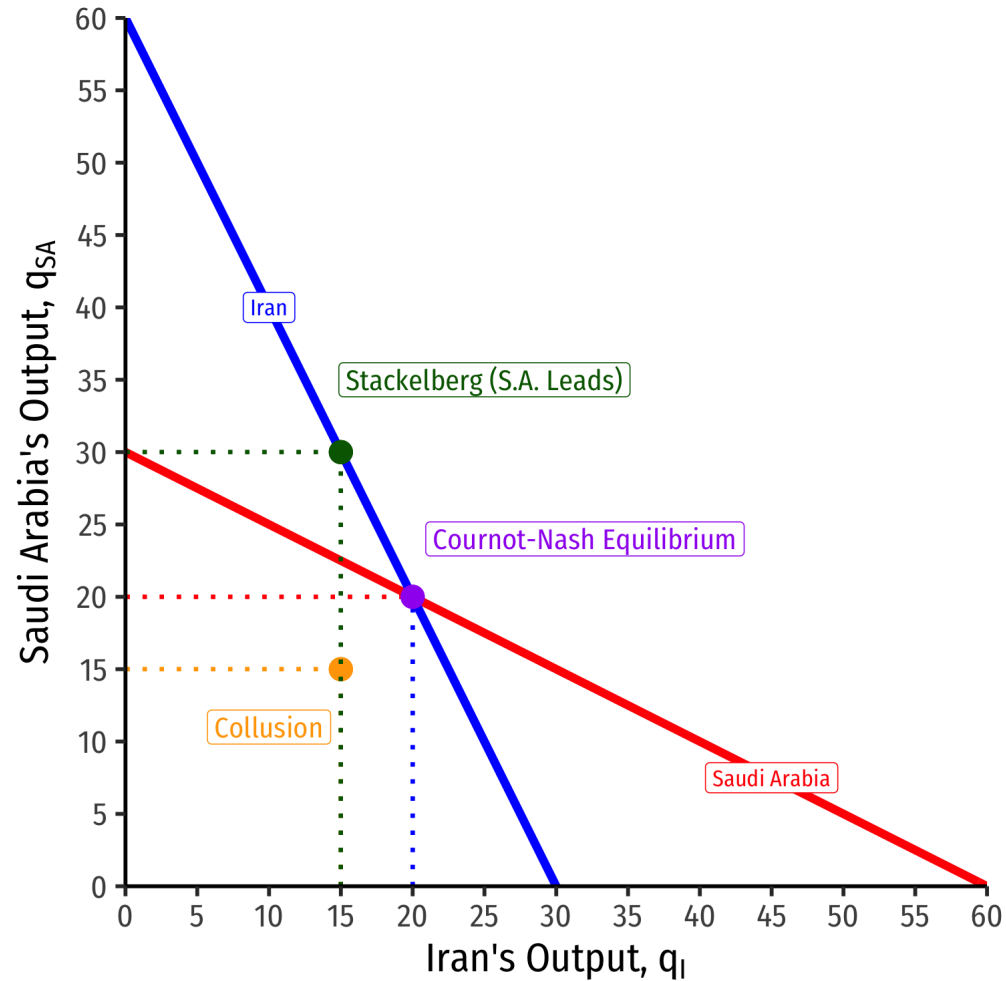
- Now **Saudi Arabia** can find its optimal quantity:

$$\begin{aligned}MR_{Leader} &= MC \\110 - 3q_{sa} &= 20 \\30 &= q_{sa}^*\end{aligned}$$

- **Iran** will optimally respond by producing:

$$\begin{aligned}q_i^* &= 30 - 0.5q_{sa} \\q_i^* &= 30 - 0.5(30) \\q_i^* &= 15\end{aligned}$$

Stackelberg Equilibrium, Graphically



- **Stackelberg Nash Equilibrium:**

$$(q_{sa}^* = 30, q_i^* = 15)$$

Stackelberg Competition: Example



- With $q_{sa}^* = 30$ and $q_i^* = 15$, this sets a market-clearing price of:

$$P = 200 - 3(45)$$

$$P = 65$$

- **Saudi Arabia's** profit would be:

$$\pi_{sa} = 30(65 - 20)$$

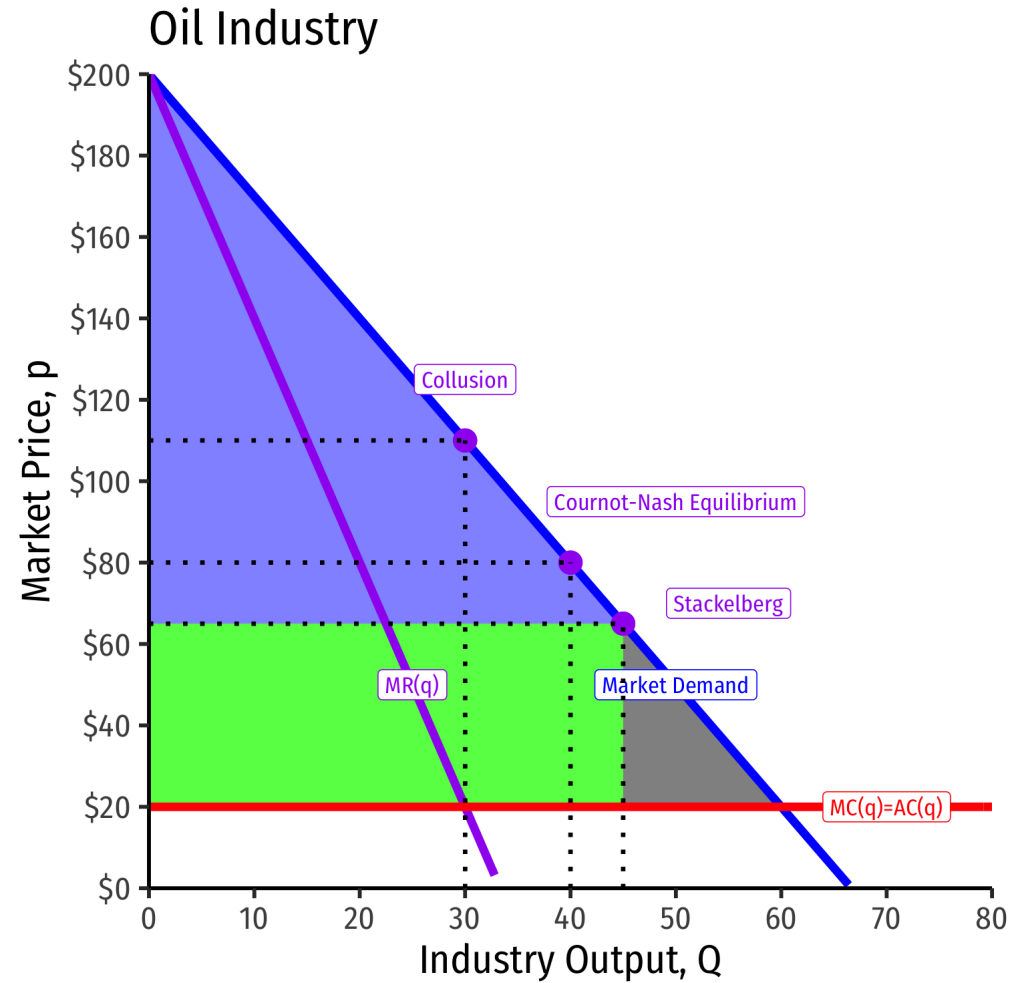
$$\pi_{sa} = \$1,350$$

- **Iran's** profit would be:

$$\pi_i = 15(65 - 20)$$

$$\pi_i = \$675$$

Stackelberg Equilibrium, The Market



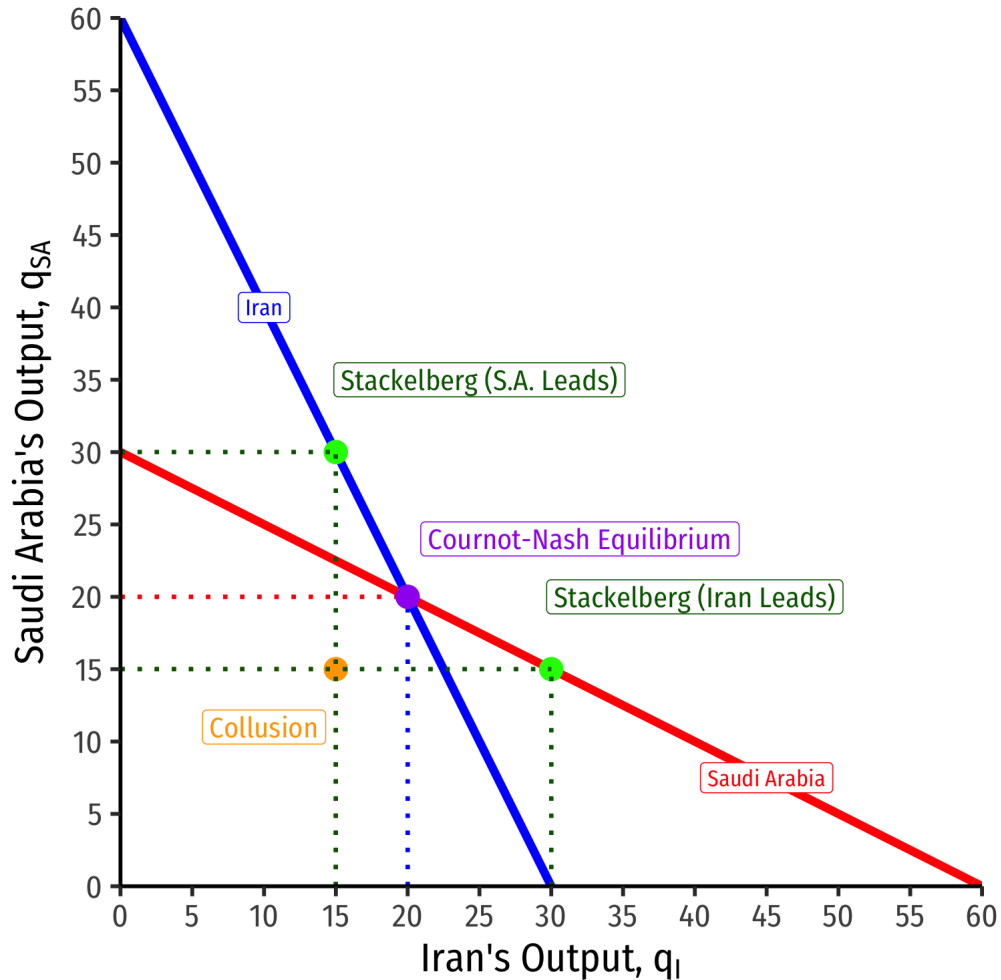
Cournot vs. Stackelberg Competition



Firm	Cournot ($p^*=\$80$)		Stackelberg ($p^*=\$65$)	
	Output	Profit	Output	Profit
Saudi Arabia	20	\$1,200	30	\$1,350
Iran	20	\$1,200	15	\$675
Industry	40	\$2,400	45	\$2,025

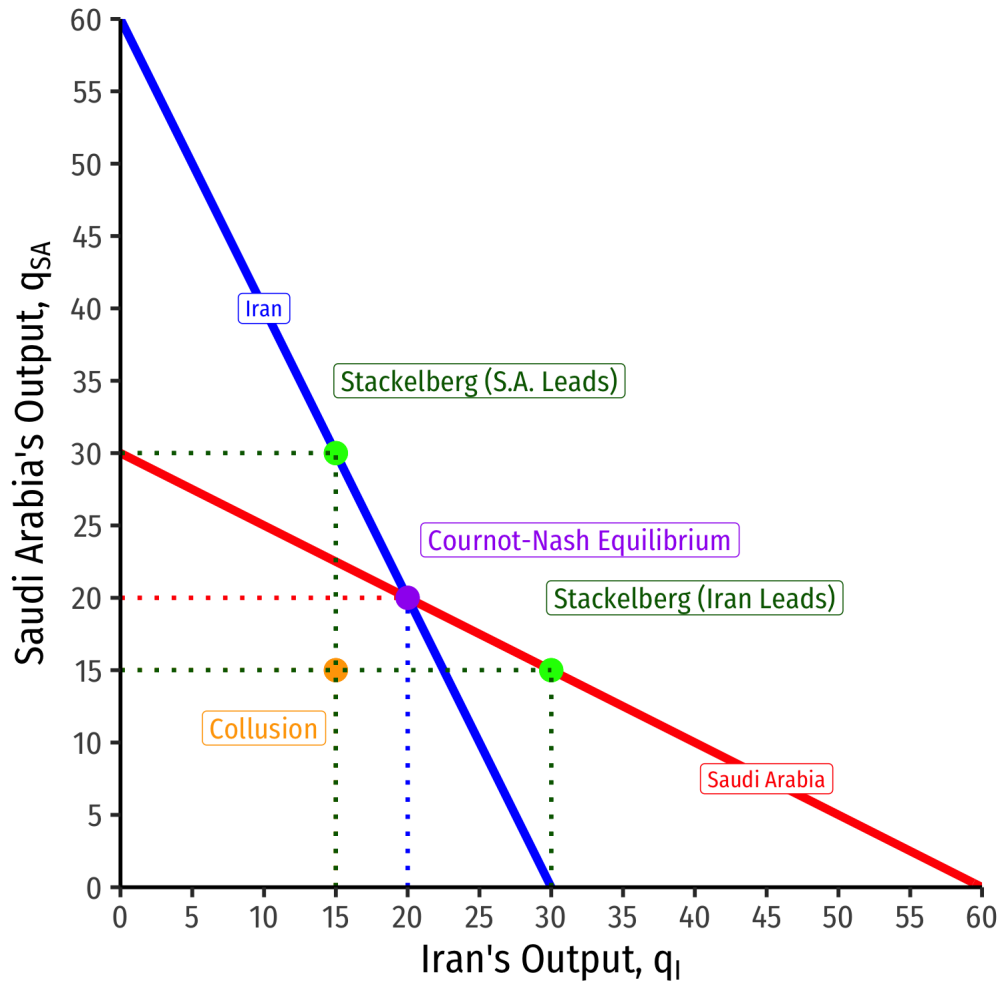
- **Leader** Saudi Arabia \uparrow its output and \uparrow profits
- **Follower** Iran forced to \downarrow its output and accept \downarrow profits

Stackelberg and First-Mover Advantage



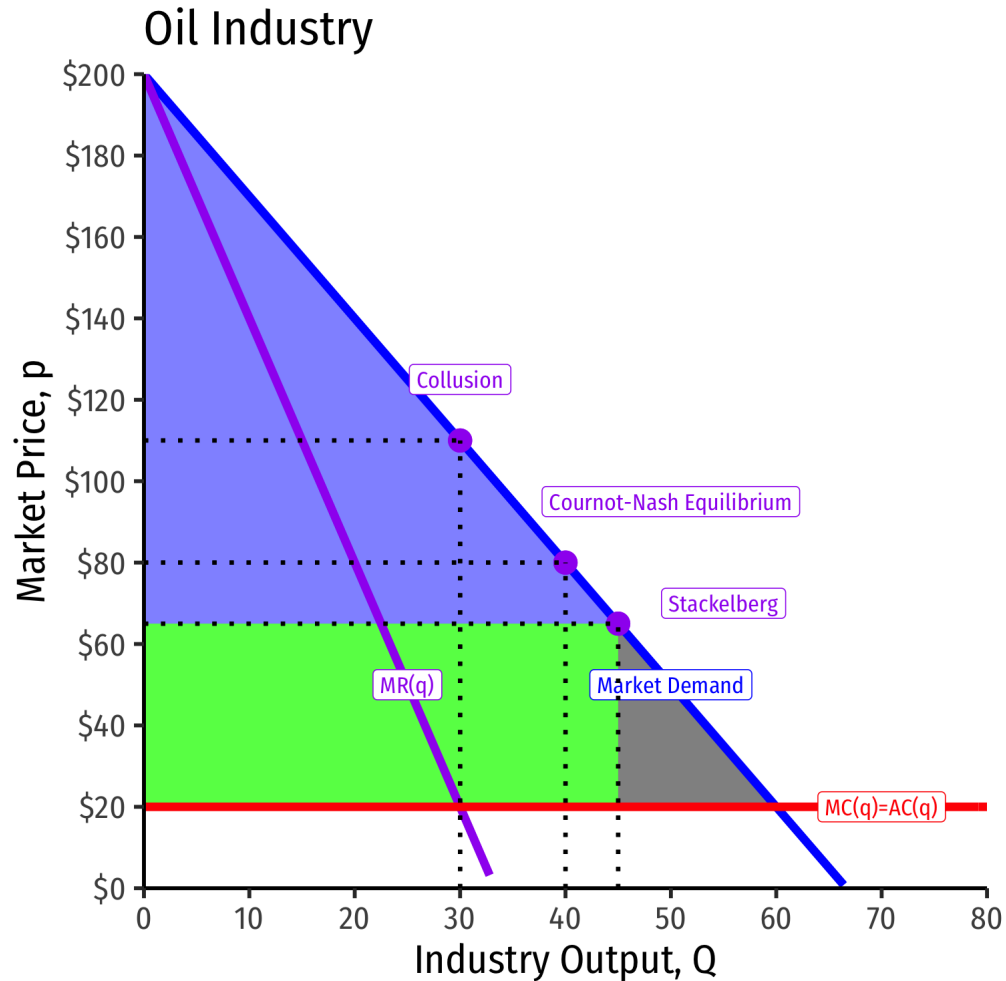
- Stackelberg **leader** clearly has a **first-mover advantage** over the **follower**
 - **Leader:** $q^* = 30, \pi = 1,350$
 - **Follower:** $q^* = 15, \pi = 675$
- If firms compete **simultaneously** (**Cournot**): $q^* = 20, \pi = 1,200$ each
- Leading \succ simultaneous \succ Following

Stackelberg and First-Mover Advantage



- Stackelberg Nash equilibrium requires **perfect information** for **both** leader and follower
 - Follower must be able to **observe** leader's output to choose its own
 - Leader must **believe** follower will see leader's output and react optimally
- **Imperfect information** reduces the game to (simultaneous) **Cournot competition**

Stackelberg and First-Mover Advantage



- Again, leader *cannot* act like a monopolist
 - A strategic game! Market output (that pushes down market price) is
$$Q = q_{sa} + q_i$$
- Leader's choice of 30 is optimal **only if** follower responds with 15

Comparing All Oligopoly Models



Country	Bertrand			Cournot			Stackelberg			Collusion		
	q	p	π	q	p	π	q	p	π	q	p	π
Saudi Arabia	30	\$20	\$0	20	\$80	\$1,200	30	\$65	\$1,350	15	\$110	\$1,350
Iran	30	\$20	\$0	20	\$80	\$1,200	15	\$65	\$675	15	\$110	\$1,350
Industry	60	\$20	\$0	40	\$80	\$2,400	45	\$65	\$2,025	30	\$110	\$2,700

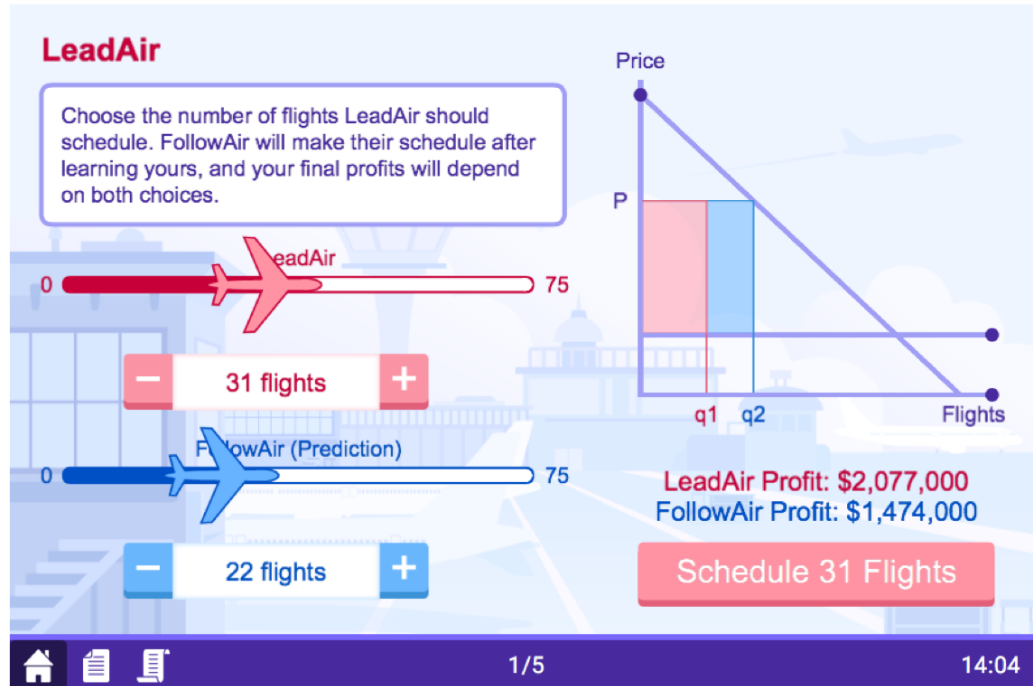
- Output: $Q_m < Q_c < Q_s < Q_b$
- Market price: $P_b < P_s < P_c < P_m$
- Profit: $\pi_b = 0 < \pi_s < \pi_c < \pi_m$

Where subscript m is monopoly (collusion), c is Cournot, s is Stackelberg, b is Bertrand

Stackelberg Competition: Moblab



Stackelberg Competition: Moblab



- Each of you is one Airline competing against another in a duopoly
 - Each pays same per-flight cost
 - Market price determined by *total* number of flights in market
- **LeadAir** first chooses its number of flights, publicly announced
- **FollowAir** then chooses its number of flights